

**CORRELATION**  
**of**  
**the 10 UNDERSTANDING MATH PLUS PROGRAMS**  
**with**  
**California State Board of Education ACADEMIC CONTENT STANDARDS**  
**For Grade 6**

**Note: a.** The Understanding Math PLUS series of programs consist of 10 programs written for Kindergarten to 10<sup>th</sup> Grade.

**The 10 programs are:**

Understanding Fractions	Understanding Whole Numbers and Integers
Understanding Probability	Understanding Percent
Understanding Exponents	Understanding Equations
Understanding Algebra	Understanding Graphing
Understanding Numeration	
Understanding Measurement and Geometry	

**Note: b.** The Understanding Numeration software for K to 3 is set up so that the teacher selects items in the following order:

Concept .. from 5 concepts .. Counting, Comparing & Ordering, Place Value, Operations and Problem Solving.

Skill .. chosen from the list of specific learning expectations

Level .. indicates the levels of development for Kindergarten to 3<sup>rd</sup> grade.

Level	Upper Range of Number
<b>A</b>	<b>10</b>
<b>B</b>	<b>20</b>
<b>C</b>	<b>100</b>
<b>D</b>	<b>1000</b>

Lesson .. 250 lessons are sequenced to build understanding of concepts.

A detailed Lesson Synopsis on the website [www.neufeldmath.com](http://www.neufeldmath.com) to assist the teacher by stating the lesson contents but also by giving lesson suggestions.

Worksheet .. off computer worksheets are selected from the CD by a code.

**Note: c.** The remaining 9 Understanding Math programs for 4<sup>th</sup> to 10<sup>th</sup> grade are set up so that they can be used in a variety of teaching and learning environments ranging from a teacher centered approach with 1 computer to a student centered lab approach. The lessons can also be used in remediation, tutorial, intervention, resource, fast-tracking.

Each topic has:

..an interactive concept introduction, usually with a variety of graphic approaches.

..a number of particular examples

..practice questions with random questions but particular feedback

..a topic test with random questions and tracking

..off computer worksheets selected from the website .. [www.neufeldmath.com](http://www.neufeldmath.com)

# Grade Six

Mathematics Content Standards.

## NUMBER SENSE

**1.0 Students compare and order positive and negative fractions, decimals, and mixed numbers. Students solve problems involving fractions, ratios, proportions, and percentages:**

Content Standard	Understanding Math PLUS computer assisted lessons
<p><b>1.1</b> Compare and order positive and negative fractions, decimals, and mixed numbers and place them on a number line.</p>	<p><b>MAT+ <u>Understanding Fractions</u></b>  <b>Topic 1: The Meaning of Fractions</b>            Fraction on a Number Line            Halves            Thirds            Quarters            Summary  <b>Topic 5: Introduction to Decimals</b>            Comparing Decimals            Examples 1,2,3,4            Ordering Decimals            Introduction            Examples 1,2,3,4</p>
<p><b>1.2</b> Interpret and use ratios in different contexts (e.g., batting averages, miles per hour) to show the relative sizes of two quantities, using appropriate notations ( <math>a/b</math>, <math>a</math> to <math>b</math>, <math>a:b</math> ).</p>	<p><b>MAT+ <u>Understanding Percent</u></b>  <b>Topic 4: Ratios and Proportions</b>            Ratios in the News            What is a Ratio            Examples            1. Fraction Strip            2. Balls            3. Students            4. Gears            Writing Ratios            Concept            Examples 1,2,3,4</p>
<p><b>1.3</b> Use proportions to solve problems (e.g., determine the value of <math>N</math> if <math>4/7 = N/21</math>, find the length of a side of a polygon similar to a known polygon). Use cross-multiplication as a method for solving such problems, understanding it as the multiplication of both sides of an equation by a multiplicative inverse.</p>	<p><b>MAT+ <u>Understanding Percent</u></b>  <b>Topic 4: Ratios and Proportions</b>            What is Proportion?            Proportions            Example 1            Example 2- Lemonade            Example 3 – Marbles            Example 4 – Trout            Example 5 – Tree Height            Example 6 – Map            Example 7 – Scale Drawing</p>
<p><b>1.4</b> Calculate given percentages of quantities and solve problems involving discounts at sales, interest earned, and tips.</p>	<p><b>MAT+ <u>Understanding Percent</u></b>  <b>Topic 7: Percent in Business</b>            In This Topic            Sales Tax            Bicycle Question            Coat Question            Restaurant Tipping            Discount            Football Sale</p>

	<p>What Can I Afford? Which is Cheaper? Competitor's Discount Simple Interest What is it? Complete the Table Bank Interest Credit Card Bill</p>
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**2.0 Students calculate and solve problems involving addition, subtraction, multiplication, and division:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<p><b>2.1</b> Solve problems involving addition, subtraction, multiplication, and division of positive fractions and explain why a particular operation was used for a given situation.</p>	<p><b>MAT+ <u>Understanding Fractions</u></b>  <b>Topic 8: Adding Fractions</b>            Word Problems                Alexander's Friends                Eating Candy                Goal Scoring                Taking a Walk</p> <p><b>Topic 9: Subtracting Fractions</b>            Word Problems                Pedro and Alex Race                Washing the Cars                Planting a Garden</p> <p><b>Topic 10: Multiplying Fractions</b>            Word Problems                Boris' Money                Maria's Trip            A Summary            The Meaning of "OF"            Order in Multiplying                Examples 1,2            Multiplying Fractions with Large Numbers                Examples 1,2</p> <p><b>Topic 14: Dividing Fractions</b>            Examples without Diagrams                Numerical Examples 1,2                Central High School</p>
<p><b>2.2</b> Explain the meaning of multiplication and division of positive fractions and perform the calculations (e.g., <math>5/8 \div 15/16 = 5/8 \times 16/15 = 2/3</math>).</p>	<p><b>Topic 10: Multiplying Fractions</b>            Pattern Blocks                Hexagons 1,2,3            Fractions Strips                Concepts 1,2            Word Problems                Boris' Money                Maria's Trip            A Summary            The Meaning of "OF"            Order in Multiplying                Examples 1,2</p> <p><b>Topic 14: Dividing Fractions</b>            Understanding Division            Examples with Diagrams                Soda Pop</p>

	Ice Cream Shapes 1 & 2 Patterns from Examples Another Explanation Examples 1 & 2
<b>2.3</b> Solve addition, subtraction, multiplication, and division problems, including those arising in concrete situations, that use positive and negative integers and combinations of these operations.	<b>MAT+ <u>Understanding Whole Numbers and Integers</u></b> <b>Topic 5: Adding Integers</b> Word Problems Temperature Money Car Practice Questions; Topic Test  <b>Topic 6: Subtracting Integers</b> Example Questions Example 1 – With Brackets Example 2 – With Brackets Example 3 – Meaning of ...2-5 Example 4 – Meaning of -7-3 Example 5 – Meaning of -7+9-18 Example 6 – Meaning of -4-9+2-8 Summary from Examples 3 to 6 Word Problems The Sailboat The Bank Practice Questions; Topic Test  <b>Topic 7: Multiplying Integers</b> Word Problems Washing Cars The Helicopter Construction Practice Questions; Topic Test  <b>Topic 8: Dividing Integers</b> Word Problems Casino Plant Graham’s Walk Practice Questions; Topic Test
<b>2.4</b> Determine the least common multiple and the greatest common divisor of whole numbers; use them to solve problems with fractions (e.g., to find a common denominator to add two fractions or to find the reduced form for a fraction).	<b>MAT+ <u>Understanding Fractions</u></b> <b>Topic 3: Equivalent Fractions</b> Greatest Common Factor 12 and 18 30 and 40 70 and 42 Simplifying Fractions to Simplest Form Methods 1,2

## ALGEBRA AND FUNCTIONS

**1.0 Students write verbal expressions and sentences as algebraic expressions and equations; they evaluate algebraic expressions, solve simple linear equations, and graph and interpret their results:**

Content Standard	Understanding Math PLUS computer assisted lessons
<b>1.1</b> Write and solve one-step linear equations in one variable.	<b>MAT+ <u>Understanding Equations</u></b> <b>Topic 2: Solving One-step Equations</b> Our Problem Concepts – Examples with Tiles

	<p>Examples 1 through 4          Concepts – Examples without Tiles          Practice Questions; Topic Test</p> <p><b>MAT+ <u>Understanding Graphing</u></b>          In This Topic          What is a Linear Relation?          Graphs of Linear Relations          Concept          Examples 1 through 6</p>
<p><b>1.2</b> Write and evaluate an algebraic expression for a given situation, using up to three variables.</p> <p><b>1.3</b> Apply algebraic order of operations and the commutative, associative, and distributive properties to evaluate expressions; and justify each step in the process.</p>	<p><b>MAT+ <u>Understanding Algebra</u></b>  <b>Topic 4: Patterns, Formulas, Substitution</b>          Introduction...Math is Patterns          Expressions, Terms, Variables          Definitions          Summary          Patterns to Formulas          Example...Hockey Standings          Example...Counting Money          Example...Angles in a Polygon          Substitution is...Math Scrabble          Scrabble 1,2,3          Challenge          Substitution Examples          Examples 1,2,3,4</p>
<p><b>1.4</b> Solve problems manually by using the correct order of operations or by using a scientific calculator.</p>	<p><b>MAT+ <u>Understanding Whole Numbers and Integers</u></b>  <b>Topic 9: Order of Operations</b>          Why use Order of Operations?          BEDMAS          Example Questions          Examples 1 through 10          Word Problems          Shipping          Babysitting          Garbage</p>

**2.0 Students analyze and use tables, graphs, and rules to solve problems involving rates and proportions:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<p><b>2.1</b> Convert one unit of measurement to another (e.g., from feet to miles, from centimeters to inches).</p>	<p><b>MAT+ <u>Understanding Measurement and Geometry</u></b>  <b>Topic 1: An Introduction to Measurement</b>          Measurement in the News          A Glimpse into the Past          Metric and US Standard Measurement          Searching for Standardized Measurements          Related Units from Metric Prefixes          Metric Prefixes at Work          Converting Between Metric Units</p>
<p><b>2.2</b> Demonstrate an understanding that <i>rate</i> is a measure of one quantity per unit value of another quantity.</p>	
<p><b>2.3</b> Solve problems involving rates, average speed, distance, and time.</p>	

**3.0 Students investigate geometric patterns and describe them algebraically:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted</b>
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	<b>lessons</b>
<p><b>3.1</b> Use variables in expressions describing geometric quantities (e.g., <math>P = 2w + 2l</math>, <math>A = 1/2bh</math>, <math>C = \pi d</math> - the formulas for the perimeter of a rectangle, the area of a triangle, and the circumference of a circle, respectively).</p>	<p><b>MAT+ <u>Understanding Measurement and Geometry</u></b>  <b>Topic 2: Perimeter and Area of Polygons</b>  Walk Around a Polygon  Joan Walks  Perimeter of Various Shapes  Perimeter of the Ranch  Length of the Metal Strip  Find the Perimeter  Amount of Surface  The Driveway – An Introduction to Area  Area – Estimation  Area of a Rectangle  Area of a Parallelogram  Area of a triangle  Relationship – Area and Perimeter  Squares  Rectangles  Given Area and Perimeter – Create Shapes  Examples 1, 2, 3, 4</p> <p><b>Topic 3: The Circle</b>  Radius, Circumference, Diameter  PI...A Special Number  Introduction  How do we Measure Circumference?  Measuring Circles  Summary</p>
<p><b>3.2</b> Express in symbolic form simple relationships arising from geometry.</p>	<p><b>MAT+ <u>Understanding Measurement and Geometry</u></b>  <b>Topic 2: Perimeter and Area of Polygons</b>  Given Area and Perimeter – Create Shapes  Examples 1, 2, 3, 4  Problems Section  Length of Fence  Area of a Wall  The Tablecloth</p>

## MEASUREMENT AND GEOMETRY

**1.0 Students deepen their understanding of the measurement of plane and solid shapes and use this understanding to solve problems:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<p><b>1.1</b> Understand the concept of a constant such as <math>\pi</math>; know the formulas for the circumference and area of a circle.</p> <p><b>1.2</b> Know common estimates of <math>\pi</math> (3.14; 22/7) and use these values to estimate and calculate the circumference and the area of circles; compare with actual measurements.</p>	<p><b>MAT+ <u>Understanding Measurement and Geometry</u></b>  <b>Topic 3: The Circle</b>  Circumference of a Circle  Circumference  Example 1 – Egg  Example 2 – The Well  Example 3 – The Rolling Coin  Example 4 – The Semi-Circle  Area of a Circle  Recall Area  Area Exploration #1, #2  Example 1 – Wheel  Example 2 – Pizza  Example 3 – The Semi-circle  Example 4 – The Dog’s Run  Example 5 – The Hockey Rink</p>

<p><b>1.3</b> Know and use the formulas for the volume of triangular prisms and cylinders (area of base x height); compare these formulas and explain the similarity between them and the formula for the volume of a rectangular solid.</p>	<p><b>MAT+ <u>Understanding Measurement and Geometry</u></b>  <b>Topic 4: Solids: Volume and Surface Area</b>  Volume of a Solid  The Concept  Volume of a Prism: Examples 1, 2  Volume of a Cylinder</p>
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**2.0 Students identify and describe the properties of two-dimensional figures:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<p><b>2.1</b> Identify angles as vertical, adjacent, complementary, or supplementary and provide descriptions of these terms.</p> <p><b>2.2</b> Use the properties of complementary and supplementary angles and the sum of the angles of a triangle to solve problems involving an unknown angle.</p>	<p><b>MAT+ <u>Understanding Measurement and Geometry</u></b>  <b>Topic 6: Angles and Polygons</b>  In This Topic  Parallel Lines  Example with Parallel Lines  Examples 1,2  Angles in Triangles  Exploration  An Explanation  Exterior Angles – Example  Angles in Polygons  Methods 1,2  Exterior Angles in a Polygon  Practice Questions; Topic Test</p>
<p><b>2.3</b> Draw quadrilaterals and triangles from given information about them (e.g., a quadrilateral having equal sides but no right angles, a right isosceles triangle).</p>	

**STATISTICS, DATA ANALYSIS, AND PROBABILITY**

**1.0 Students compute and analyze statistical measurements for data sets:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<p><b>1.1</b> Compute the range, mean, median, and mode of data sets.</p> <p><b>1.2</b> Understand how additional data added to data sets may affect these computations of measures of central tendency.</p> <p><b>1.3</b> Understand how the inclusion or exclusion of outliers affects measures of central tendency.</p> <p><b>1.4</b> Know why a specific measure of central tendency (mean, median, mode) provides the most useful information in a given context.</p>	<p><b>MAT+ <u>Understanding Graphing</u></b>  <b>Topic 2: Statistics</b>  Measures of Central Tendency  Introduction  The Mean Average  The Median Average  The Mode  Summary  Another Example  Adding Data Points</p>

**2.0 Students use data samples of a population and describe the characteristics and limitations of the samples:**

Content Standard	Understanding Math PLUS computer assisted lessons
2.1 Compare different samples of a population with the data from the entire population and identify a situation in which it makes sense to use a sample.	
2.2 Identify different ways of selecting a sample (e.g., convenience sampling, responses to a survey, random sampling) and which method makes a sample more representative for a population.	
2.3 Analyze data displays and explain why the way in which the question was asked might have influenced the results obtained and why the way in which the results were displayed might have influenced the conclusions reached.	
2.4 Identify data that represent sampling errors and explain why the sample (and the display) might be biased.	
2.5 Identify claims based on statistical data and, in simple cases, evaluate the validity of the claims.	

**3.0 Students determine theoretical and experimental probabilities and use these to make predictions about events:**

Content Standard	Understanding Math PLUS computer assisted lessons
3.1 Represent all possible outcomes for compound events in an organized way (e.g., tables, grids, tree diagrams) and express the theoretical probability of each outcome.	<b>MAT+ <u>Understanding Probability</u></b> <b>Topic 1 .. An Introduction to Probability</b> The Language of Chance Impossible to Certain Activity 1 Activity 2 Probability Lines Line 1 Line 2 Experiments with Spinners Experiment 1, Experiment 2 .... Experiment 6 The Spinner Game Board 1 Board 2 IT's in the Bag Tree Diagrams Meals Socks
3.2 Use data to estimate the probability of future events (e.g., batting averages or number of accidents per mile driven).	
3.3 Represent probabilities as ratios, proportions, decimals between 0 and 1, and percentages between 0 and 100 and verify that the probabilities	

computed are reasonable; know that if $P$ is the probability of an event, $1 - P$ is the probability of an event not occurring.	
<b>3.4</b> Understand that the probability of either of two disjoint events occurring is the sum of the two individual probabilities and that the probability of one event following another, in independent trials, is the product of the two probabilities.	<b>MAT+ <u>Understanding Probability</u></b> <b>Topic 7: Independent Events</b> In This Topic What are They? Examples 1,2
<b>3.5</b> Understand the difference between independent and dependent events.	<b>MAT+ <u>Understanding Probability</u></b> <b>Topic 7: Independent Events</b> In This Topic What are They? Examples 1,2  <b>Topic 8: Dependent Events</b> In This Topic What Are They? Independent Events Dependent Events Examples 1,2 Probability – Examples 1,2,3

## MATHEMATICAL REASONING

### 1.0 Students make decisions about how to approach problems:

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<b>1.1</b> Analyze problems by identifying relationships, distinguishing relevant from irrelevant information, identifying missing information, sequencing and prioritizing information, and observing patterns.	<b>Understanding Math PLUS...all programs</b>
<b>1.2</b> Formulate and justify mathematical conjectures based on a general description of the mathematical question or problem posed.	<b>Understanding Math PLUS...all programs</b>
<b>1.3</b> Determine when and how to break a problem into simpler parts.	<b>Understanding Math PLUS...all programs</b>

### 2.0 Students use strategies, skills, and concepts in finding solutions:

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<b>2.1</b> Use estimation to verify the reasonableness of calculated results.	
<b>2.2</b> Apply strategies and results from simpler problems to more complex problems.	<b>Understanding Math PLUS...all programs</b>
<b>2.3</b> Estimate unknown quantities graphically and solve for them by using logical reasoning and arithmetic and algebraic techniques.	
<b>2.4</b> Use a variety of methods, such as words, numbers, symbols, charts, graphs, tables, diagrams, and	<b>MAT+ <u>Understanding Equations</u></b> <b>Topic 5: Word Problems</b>

<p>models, to explain mathematical reasoning.</p> <p><b>2.5</b> Express the solution clearly and logically by using the appropriate mathematical notation and terms and clear language; support solutions with evidence in both verbal and symbolic work.</p>	<p>Words and Symbols  The Translation Machine  Examples 1,2,3,4  The Trick Machine  Instructions  The Machine  Explanation with Picture; with Symbols  Area of Walls  Chemistry  Pools Puzzler – The First Problem  Perimeter Problem with Diagram  Money Problem with Chart  Age Problem with Chart  Buying CDs  Meat Mixture  Coffee Mixture  Rate of Work  Summary: Problem Solving Using Equations  Practice Questions; Topic Test</p>
<p><b>2.6</b> Indicate the relative advantages of exact and approximate solutions to problems and give answers to a specified degree of accuracy.</p>	
<p><b>2.7</b> Make precise calculations and check the validity of the results from the context of the problem.</p>	

**3.0 Students move beyond a particular problem by generalizing to other situations:**

<b>Content Standard</b>	<b>Understanding Math PLUS computer assisted lessons</b>
<p><b>3.1</b> Evaluate the reasonableness of the solution in the context of the original situation.</p>	
<p><b>3.2</b> Note the method of deriving the solution and demonstrate a conceptual understanding of the derivation by solving similar problems.</p>	
<p><b>3.3</b> Develop generalizations of the results obtained and the strategies used and apply them in new problem situations.</p>	